

# Colloidally Stable Germanium Nanocrystals for Photonic Applications

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Semiconductor nanocrystals have captivated the imagination of scientists and engineers since their technological potential became evident over 2 decades ago. This is especially true for semiconductor quantum dots, in which quantum size effects and carrier confinement allow unprecedented control over optical and electronic properties.<sup>1</sup> Illuminating the way in this field, in both theoretical understanding and demonstrated applications, is indisputably the cadmium chalcogenide based II–VI quantum dots originally discovered by Brus.<sup>2</sup> However, legitimate concerns regarding their toxicity have yet to be resolved,<sup>3</sup> pressing for the advancement of alternate nontoxic technologies, including the group 14 semiconductor nanocrystals.<sup>4</sup>

Although silicon is the leader of the group 14 nanocrystal congeners, germanium (Ge) offers unique opportunities that are actively being pursued, especially for charge storage and infrared optical and optoelectronic applications.<sup>5–7</sup> Similarly to most semiconductor nanocrystals, focus has primarily been on Ge quantum dots, where size-dependent optical and electronic properties have been investigated mostly for optoelectronic or *in vivo* biological imaging applications.<sup>8,9</sup> However, what is perhaps an overlooked “nano advantage” is the solution-processability of colloidally stable nanomaterials for the production of structures which retain bulk properties, offering attractive alternatives to typical top-down fabrication techniques. Inexpensive, scalable, using nontoxic and easy to handle precursors, and requiring minimal infrastructure, spin-coating, dip-coating, and spray-coating, to name but a few, are certainly appealing thin film deposition meth-

**ABSTRACT** We report the development of a straightforward synthesis for colloidally stable germanium nanocrystals for use as a solution-processable precursor for the bottom-up fabrication of functional thin films. SiO<sub>2</sub>-embedded germanium nanocrystals are produced by the reductive thermal processing of sol–gel glasses derived from mixtures of tetraethoxyorthogermanate (TEOG) and tetraethoxyorthosilicate (TEOS), and free-standing germanium nanocrystals are liberated from the encapsulating silicon dioxide through sequential chemical etching. The applicability of these germanium nanocrystals as a solution-processable thin film precursor is demonstrated by the fabrication of high refractive index thin films.

**KEYWORDS:** germanium · nanocrystals · sol–gel chemistry · thin films · refractive index · solution-processable · spin-coating

ods, as long as the properties of the final material are suitable for the desired application. The applicability of this strategy has recently been demonstrated by the formation of highly conductive thin films and thin film transistors (TFTs) from solution-processable plasma-synthesized germanium nanocrystals (Ge-NCs).<sup>10,11</sup>

Since the first reports of luminescent Ge-NCs in 1991,<sup>12</sup> many syntheses have emerged based on surfactant/solvent-assisted solution reductions,<sup>6,13–18</sup> metathesis reactions,<sup>19–21</sup> supercritical thermolysis,<sup>22,23</sup> solution-phase thermal decomposition,<sup>24–26</sup> gas-phase plasma decomposition,<sup>27</sup> and solid-state thermolysis.<sup>28,29</sup> In almost all cases, emphasis has been placed on developing methods of controlling the average size of the Ge-NCs as well as obtaining narrow size distributions. This is not surprising given that the majority of foreseen applications for Ge-NCs, including optical, optoelectronic, and charge storage, are not only sensitive to the NC size but also to the size distribution.<sup>30</sup> As a result of these considerations, great care is taken during synthesis to ensure size uniformity, which oftentimes results in the use of elaborate experimental setups,

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specialized reagents, surfactants, extensive cleaning, and lengthy precipitation steps.

As an example, consider the synthesis of SiO<sub>2</sub>-embedded Ge-NCs, a system which continues to generate great interest for charge storage applications (*i.e.*, flash memory).<sup>5,31,32</sup> The vast majority of the reported syntheses are based on physical methods such as ion implantation,<sup>33</sup> chemical vapor deposition,<sup>34</sup> and co-sputtering.<sup>35</sup> However, a very elegant alternative synthetic method involves the co-hydrolysis and co-condensation of Si and Ge sol–gel precursors to form Si–Ge mixed oxide glasses. Considering that all of these methods require annealing in inert or H<sub>2</sub>-containing atmospheres to reduce GeO<sub>2</sub> to Ge (in the case of H<sub>2</sub> atmospheres), initiate Ge diffusion through the encapsulating SiO<sub>2</sub> matrix, clustering of Ge atoms, and eventual crystallization of Ge-NCs, it is surprising that the sol–gel approach is not as frequently used. Such sol–gel systems can offer tremendous opportunities for NC size control, either by exploiting the compositional versatility of sol–gel chemistry or through simple changes to processing conditions (*i.e.*, peak temperature and time).<sup>36–38</sup> In order to obtain a narrow Ge-NC size distribution from the thermal processing of these sol–gel copolymers, their ideal structure would consist of a homogeneous distribution of Ge atoms throughout the copolymer. The first report of SiO<sub>2</sub>-embedded Ge-NCs formed *via* sol–gel copolymers employed mixtures of GeCl<sub>4</sub> and Si(OEt)<sub>4</sub> (TEOS),<sup>39</sup> but the very fast hydrolysis rate of GeCl<sub>4</sub> relative to TEOS led to difficulties in making solid solutions, controlling the nucleation and growth reaction, and therefore the resulting size and size distribution of the Ge-NCs.<sup>40</sup> In order to overcome this kinetic obstacle, variations to the Ge sol–gel precursors have been used to slow the hydrolysis rate, using 3-trichlorogermanium propionic acid (Cl<sub>3</sub>–Ge–C<sub>2</sub>H<sub>4</sub>–CO<sub>2</sub>H) in particular.<sup>36–38,40</sup> Similar kinetic differences are likely the reason why combinations of the typical (and inexpensive) sol–gel precursors Ge(O–Et)<sub>4</sub> (TEOG) and Si(OEt)<sub>4</sub> (TEOS) have not been used for SiO<sub>2</sub>-embedded Ge-NCs. The greater hydrolysis rate of TEOG<sup>41</sup> would lead to GeO<sub>2</sub> clustering during co-hydrolysis and co-condensation and ultimately result in an inhomogeneous distribution (phase separation) of Ge throughout the sol–gel copolymer. This is especially surprising given the wealth of examples using TEOG/TEOS sol–gel for the formation of compositionally homogeneous index-controlled optical fibers.<sup>41</sup> Therefore, the necessity of controlled size and narrow size distribution in these advanced applications has the added cost of exotic precursors and elaborate reaction conditions, which removes the elegant simplicity of the sol–gel process.

There are, of course, applications that exploit the “nano-advantage” without being held hostage to size effects, and for these, the nanoparticle synthesis becomes much more straightforward. For example, it has

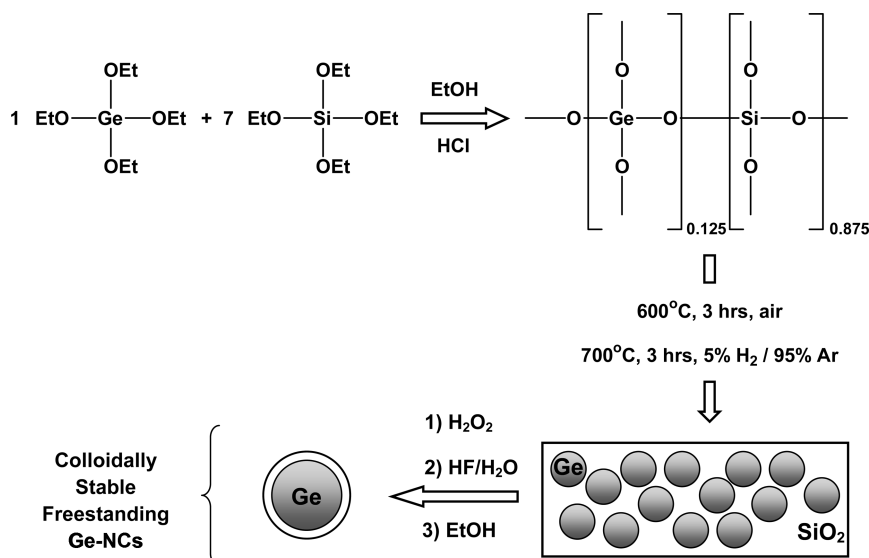
recently been shown that dielectric nanoparticle suspensions can be used as solution-processable precursors for the bottom-up fabrication of porous distributed Bragg reflectors (Bragg mirrors).<sup>42</sup> Using commercially available nanoparticle suspensions with size distributions up to 20%, high quality Bragg mirrors have been fabricated with reflectance approaching 100%. As the nanoscaling laws and quantum size effects that govern optical and electronic phenomena in semiconductor quantum dots do not appreciably affect the dispersion relations of dielectrics in the visible spectrum to the same extent, narrow nanoparticle size distributions become less of a priority. In fact, broad size distributions could even lead to higher fill fractions and greater effective refractive indices. With a bulk refractive index  $n > 4$ , germanium has the potential to contribute greatly to the photonics field, especially with the development of colloidal, solution-based thin film fabrication techniques.

Here we present for the first time the synthesis of free-standing Ge-NCs obtained from the thermal processing of TEOG/TEOS sol–gel copolymers and their application as a solution-processable colloiddally stable precursor for photonic applications. A sol–gel glass was synthesized *via* co-hydrolysis and co-condensation of TEOG and TEOS, and no special considerations were taken to control relative reaction rates. After aging and drying, thermal processing in a slightly reducing atmosphere resulted in the formation of a dark red/black powder from which Ge-NCs were liberated by sequential chemical etching steps. The resulting colloiddally stable Ge-NCs were then used as a solution-processable precursor for the formation of high refractive index films.

## RESULTS AND DISCUSSION

We present the synthesis of free-standing Ge-NCs *via* the thermal reduction of GeO<sub>2</sub>/SiO<sub>2</sub> sol–gel copolymers obtained by co-hydrolysis and co-condensation of TEOG and TEOS and their use as a solution-processable colloiddally stable precursor for high refractive index thin films. With this application in mind, this synthesis is a straightforward and cost-effective alternative to comparable sol–gel preparations in which great care is taken to ensure similar hydrolysis and condensation rates of the Ge and Si precursors, usually through compositional modifications to the sol–gel precursors.<sup>38</sup> We also demonstrate for the first time how sequential chemical etching steps can be used to liberate the Ge-NCs from the encapsulating matrix and produce colloiddally stable free-standing Ge-NCs. We demonstrate the applicability of this system as a solution-processable precursor for the formation of high refractive index thin films.

The present synthetic strategy is based upon solid matrix-assisted nanocrystal formation and growth, a proven method for the preparation of various Group



**Scheme 1.** Schematic outline of Ge-NC synthesis. Acid-catalyzed hydrolysis and co-condensation of TEOG and TEOS generates a compositionally tunable  $[(\text{SiO}_2)_x(\text{GeO}_2)_y]_n$  sol-gel copolymer. In the present system, the TEOG/TEOS ratio was 1:7. After aging and drying at high temperatures in air, thermally induced reduction of  $\text{GeO}_2$  by  $\text{H}_2$  in the processing atmosphere generates elemental Ge that subsequently nucleates, grows, and crystallizes into Ge-NCs encapsulated in a  $\text{SiO}_2$  matrix. Sequential etching steps to remove bulk unencapsulated Ge and the  $\text{SiO}_2$  matrix generates free-standing Ge-NCs with mixed oxide/hydroxide/alkoxide surface termination that form stable suspensions in ethanol or methanol.

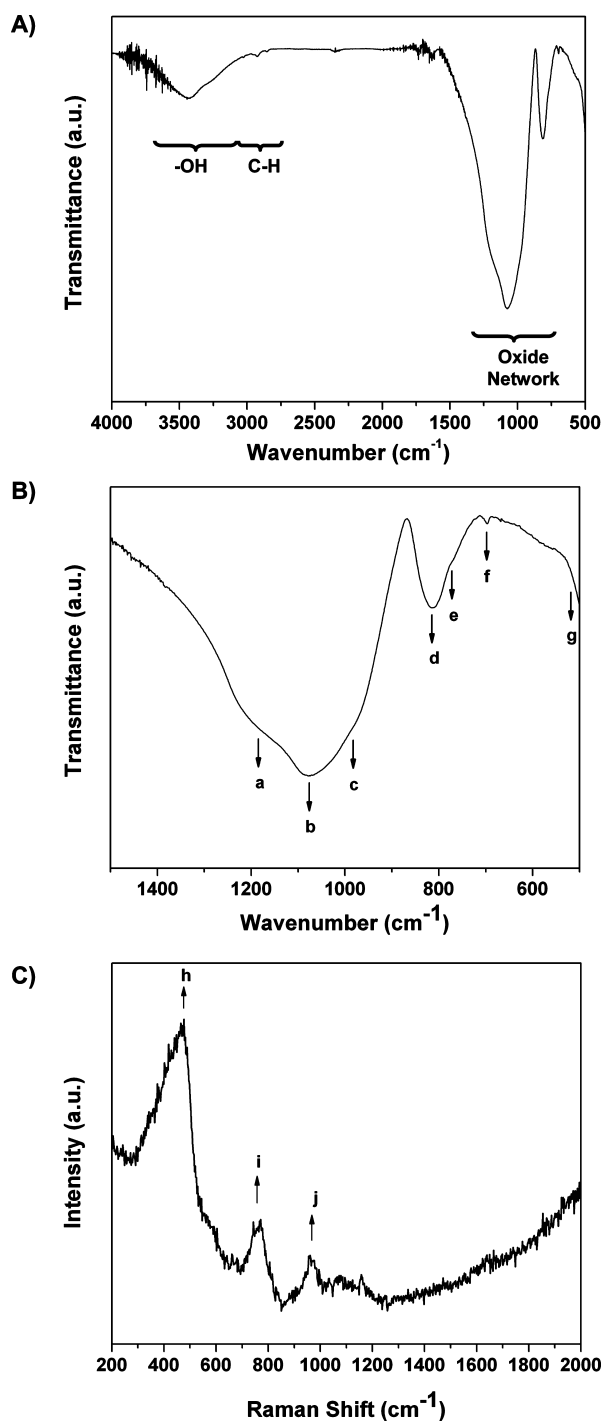
14 semiconductor nanocrystals, including Si, Ge,  $\text{Si}_{1-x}\text{Ge}_x$ , and SiC.<sup>28,43–45</sup> In these systems, a solid precursor with desired composition is prepared such that thermal initiation causes chemical transformations to the solid and activates thermodynamic driving forces that result in the diffusion of group 14 atoms throughout an inert encapsulating matrix. The matrix not only provides a temperature-resistant support for nanocluster crystallization, a key requirement for group 14 semiconductors that require high temperatures for crystallization, but also imposes kinetic diffusion barriers that can be exploited to accurately control nanocrystal formation and growth.

In the present synthesis, the formation of  $[(\text{GeO}_2)_{0.125}(\text{SiO}_2)_{0.875}]_n$  copolymers is achieved via straightforward sol-gel processing of TEOG and TEOS (Scheme 1). The compositional versatility of sol-gel chemistry can be exploited to accurately control the composition of the resulting copolymer. In this way, copolymers with TEOG/TEOS ratios of 1:3, 1:5, and 1:7 were investigated, with the latter exhibiting optimal behavior. It is well-known that the hydrolysis and condensation rates of TEOG are greater than for TEOS,<sup>41</sup> which under the present experimental conditions leads to unavoidable formation of  $\text{GeO}_2$  colloidal clusters and subsequent  $\text{GeO}_2$ -rich domains in the solid copolymer. It was found that, as the TEOG/TEOS ratio decreased, the formation of these  $\text{GeO}_2$ -rich domains was limited, as evidenced by the absence of crystalline  $\text{GeO}_2$  reflections in XRD measurements (not shown).

The composition and structure of the  $[(\text{GeO}_2)_{0.125}(\text{SiO}_2)_{0.875}]_n$  sol-gel copolymer was evaluated by Fourier transform infrared spectroscopy (FTIR) and Raman spectroscopy (Figure 1A–C). The FTIR spec-

trum (Figure 1A) is dominated by peaks centered at 1080 and 815  $\text{cm}^{-1}$  attributed to vibrations of the oxide framework, broad  $-\text{OH}$  stretching centered at 3430  $\text{cm}^{-1}$  from uncondensed  $\text{Ge}-\text{OH}$  and  $\text{Si}-\text{OH}$  groups, and low intensity  $\text{C}-\text{H}$  stretching at 2925  $\text{cm}^{-1}$  from trace amounts of unhydrolyzed  $-\text{OEt}$  groups. Detailed examination of the oxide network vibrations (Figure 1B) allows their deconvolution into numerous vibrational modes,<sup>46</sup> including  $\text{Si}-\text{O}-\text{Si}$  stretching at ca. 1180  $\text{cm}^{-1}$  (a) and ca. 1080  $\text{cm}^{-1}$  (b),  $\text{Si}-\text{O}-\text{Ge}$  stretching at ca. 980  $\text{cm}^{-1}$  (c),  $\text{Ge}-\text{O}-\text{Ge}$  stretching at ca. 980  $\text{cm}^{-1}$  (c) and 800  $\text{cm}^{-1}$  (d),  $\text{Si}-\text{O}-\text{Si}$  deformations at ca. 780  $\text{cm}^{-1}$  (e), low intensity  $\text{Si}-\text{O}-\text{Ge}$  deformations at 670  $\text{cm}^{-1}$  (f), and  $\text{Ge}-\text{O}-\text{Ge}$  deformations at ca. 520  $\text{cm}^{-1}$  (g). These assignments are further supported by Raman spectroscopy (Figure 1C) in which the symmetric  $\text{Si}-\text{O}-\text{Si}$  stretching at ca. 470  $\text{cm}^{-1}$  (h),  $\text{Ge}-\text{OH}$  stretching at 760  $\text{cm}^{-1}$  (i), and  $\text{Si}-\text{OH}$  stretching at 962  $\text{cm}^{-1}$  (j) are the prominent features. Low intensity shoulders at ca. 560  $\text{cm}^{-1}$  corresponding to  $\text{Ge}-\text{O}-\text{Si}$  and  $\text{Ge}-\text{O}-\text{Ge}$  deformations and  $\text{Ge}-\text{O}-\text{Si}$  deformations at ca. 670  $\text{cm}^{-1}$  are also present. Nearly identical spectral characteristics have been reported for  $\text{SiO}_2-\text{GeO}_2$  gels prepared under similar conditions,<sup>46</sup> and the appearance of these diagnostic bands in the FTIR and Raman spectra confirm the presence of  $\text{Si}-\text{O}-\text{Si}$ ,  $\text{Si}-\text{O}-\text{Ge}$ , and  $\text{Ge}-\text{O}-\text{Ge}$  units in the solid sol-gel copolymer.

Reductive thermal processing of the white solid  $[(\text{GeO}_2)_{0.125}(\text{SiO}_2)_{0.875}]_n$  copolymer (Figure 2A) results in  $\text{H}_2$  reduction of  $\text{GeO}_2$  to Ge and the subsequent diffusion of Ge throughout the  $\text{SiO}_2$  matrix, clustering, and eventual crystallization (Scheme 1). At this point, a dark red/black powder was obtained (Figure 2B), consisting



**Figure 1.** Characterization of  $[(\text{GeO}_2)_{0.125}(\text{SiO}_2)_{0.875}]_n$  sol-gel copolymer. (A) Fourier transform infrared (FTIR) spectrum of  $[(\text{GeO}_2)_{0.125}(\text{SiO}_2)_{0.875}]_n$  sol-gel copolymer dominated by vibrations of the oxide network, -OH stretching from uncondensed Ge-OH and Si-OH groups, and low intensity C-H stretching from unhydrolyzed -OEt group. (B) Detailed examination of the network vibrations showing characteristic Si-O-Si stretching (a and b), Si-O-Ge stretching (c), Ge-O-Ge stretching (c and d), Si-O-Si deformations (e), low intensity Si-O-Ge deformations (f), and Ge-O-Ge deformations (g). (C) Raman spectrum of  $[(\text{GeO}_2)_{0.125}(\text{SiO}_2)_{0.875}]_n$  sol-gel copolymer showing Si-O-Si stretching (h), Ge-OH stretching (i) and Si-OH stretching (j).

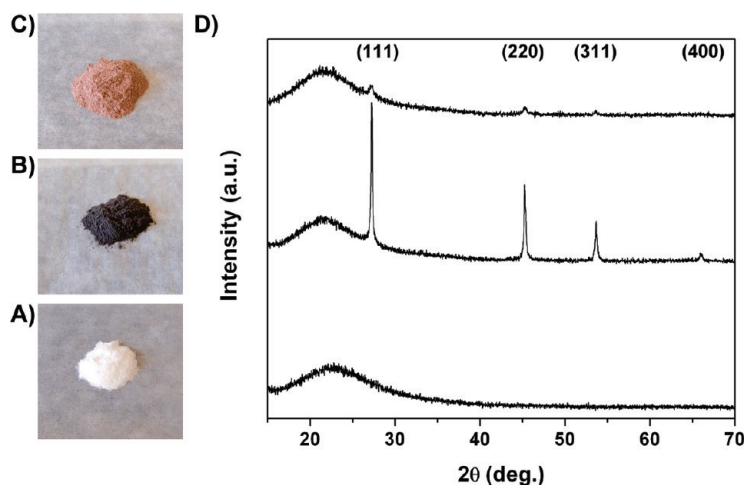
of two classes of crystalline Ge and the  $\text{SiO}_2$  matrix. Bulk crystalline Ge forms from the reduction of the aforementioned  $\text{GeO}_2$ -rich domains in the sol-gel co-

polymer and gives rise to the black color of the powder. Bulk crystals, as opposed to nanocrystals, result because their formation and growth is not directed by an encapsulating  $\text{SiO}_2$  matrix. Ge-NCs are produced from the reduction of Ge oxide species dispersed throughout the  $\text{SiO}_2$  matrix and form via a diffusion-mediated mechanism. These Ge-NCs are encapsulated within the  $\text{SiO}_2$  and give rise to the red color of the powder owing to quantum size effects on the NC band gap and absorption properties.

Although the formation of two classes of crystalline Ge could be seen as problematic, the fact that only the Ge-NCs are encapsulated within a protective  $\text{SiO}_2$  matrix can be exploited to selectively remove the bulk Ge impurities. Chemical etching of bulk Ge by aqueous  $\text{H}_2\text{O}_2$  has previously been shown to be an effective strategy for its selective dissolution from  $\text{SiO}_2$  composites.<sup>44</sup> As a result of this  $\text{H}_2\text{O}_2$  etching step, the black powder turns into a deep red powder (Figure 2C), consisting exclusively of  $\text{SiO}_2$ -encapsulated Ge-NCs.

The thermal transformation of the  $[(\text{GeO}_2)_{0.125}(\text{SiO}_2)_{0.875}]_n$  sol-gel copolymer into  $\text{SiO}_2$ -embedded Ge-NCs and subsequent removal of bulk Ge impurities was monitored by powder X-ray diffraction (PXRD) (Figure 2D). The white sol-gel precursor shows a single broad reflection in the PXRD pattern centered at *ca.*  $22^\circ$ , arising from the predominantly amorphous  $\text{SiO}_2$  network.<sup>47</sup> The formation of crystalline Ge after thermal processing at  $700^\circ\text{C}$  in 5%  $\text{H}_2$ /95% Ar to reduce the  $\text{GeO}_2$  to Ge is confirmed by the appearance of intense sharp reflections in the XRD pattern centered at *ca.*  $27$ ,  $45$ ,  $53$ , and  $66^\circ$  characteristic of the (111), (220), (311), and (400) crystal planes of diamond structure Ge.<sup>48</sup> Although the dark red/black powder contains both bulk and nanocrystalline Ge, the former dominates the XRD pattern, as diffraction peak widths are naturally biased to large crystal sizes.<sup>49</sup> After selective removal of the bulk Ge from the composite material by  $\text{H}_2\text{O}_2$  etching, a clear change in the XRD pattern is seen for the deep red powder. Broad low intensity crystalline Ge reflections appear above the amorphous background, characteristic of  $\text{SiO}_2$ -embedded Ge-NCs.

In order to liberate the Ge-NCs from the encapsulating  $\text{SiO}_2$  matrix, aqueous hydrofluoric acid (HF) solutions were used. This approach has previously been employed to liberate Ge nanostructures from  $\text{SiO}_2$ .<sup>50</sup> The etching chemistry of  $\text{SiO}_2$  by HF is well-understood and provides an effective means by which to remove the matrix. However, the effect of HF on crystalline Ge surfaces is complex and not as well-understood, with short-lived Ge-H species succumbing to oxidation and hydrolysis.<sup>51</sup> In our experience, the use of alcohol additives during etching, especially ethanol, provided excellent colloidal stability to the liberated Ge-NCs, likely through ethoxide surface passivation. Detailed investigations into the surface chemistry of these NCs is

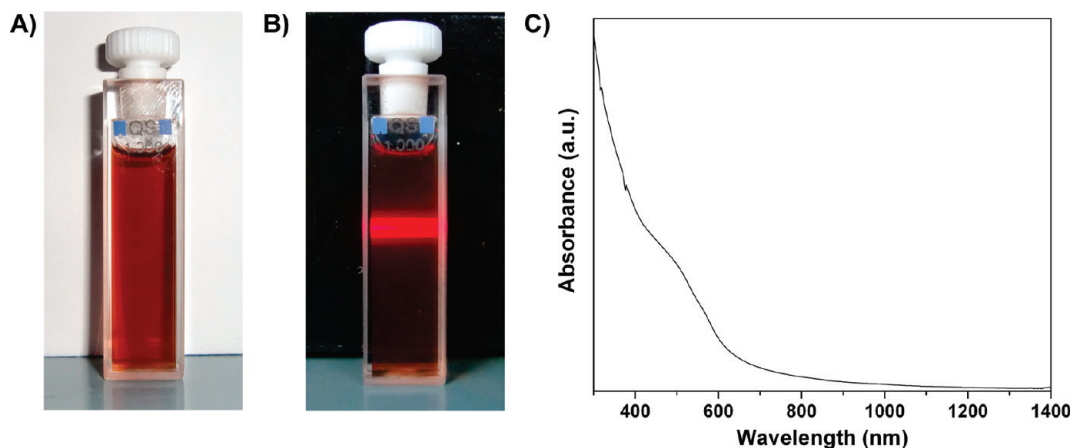


**Figure 2.** Transformation of  $[(\text{GeO}_2)_{0.125}(\text{SiO}_2)_{0.875}]_n$  sol–gel copolymer into  $\text{SiO}_2$ -embedded Ge-NCs. Picture of  $[(\text{GeO}_2)_{0.125}(\text{SiO}_2)_{0.875}]_n$  sol–gel copolymer (A) after processing at 600 °C and consisting of a  $\text{SiO}_2/\text{GeO}_2$  mixed oxide network, (B) after processing at 700 °C in 5%  $\text{H}_2/95\%$  Ar and consisting of a mixture of bulk crystalline Ge and  $\text{SiO}_2$ -encapsulated Ge-NCs, and (C) after  $\text{H}_2\text{O}_2$  etching to remove bulk crystalline Ge and consisting exclusively of  $\text{SiO}_2$ -embedded Ge-NCs. (D) Evolution of XRD pattern showing reflections characteristic of diamond structure Ge. The traces correspond to the associated samples shown in pictures A–C.

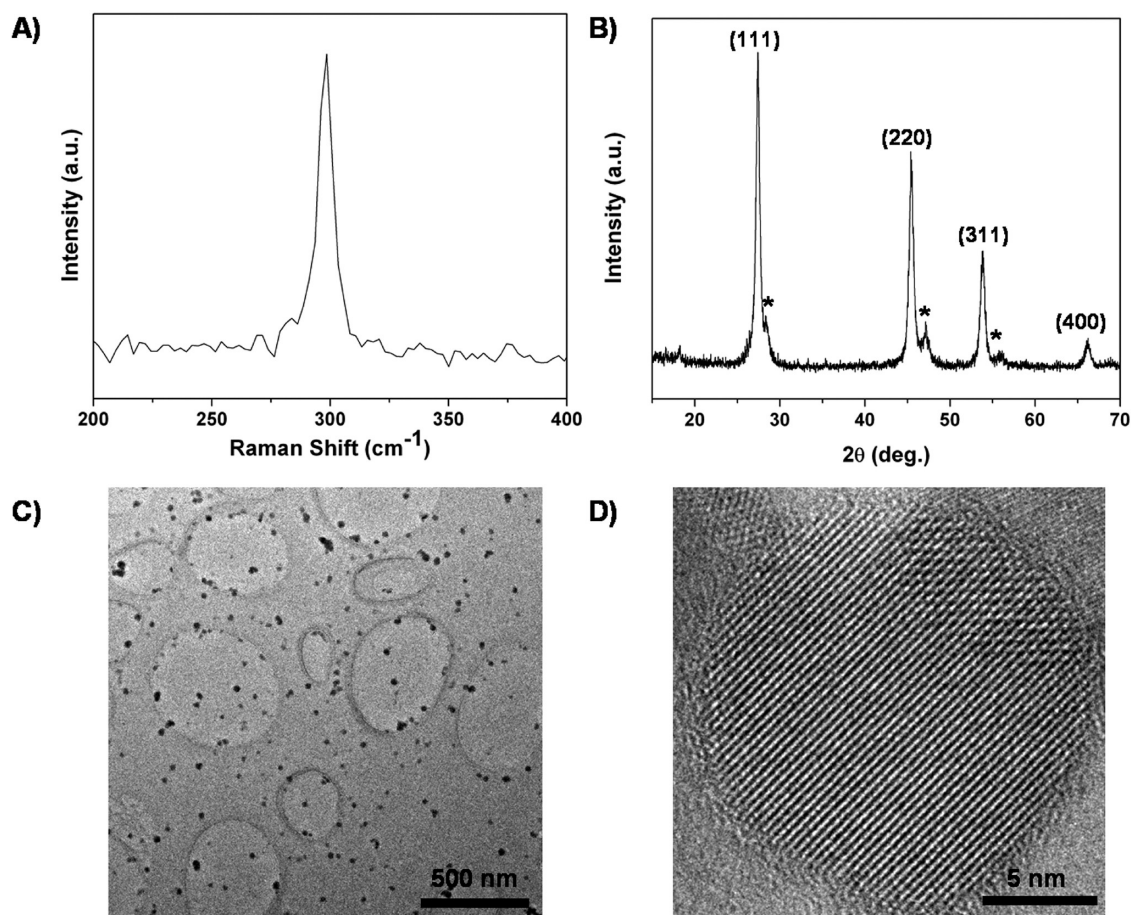
currently underway in our laboratories. The free-standing Ge-NCs form deep red colloidal suspensions in ethanol and methanol with only limited flocculation and precipitation occurring over periods of several weeks (Figure 3A,B). The absorption spectrum (Figure 3C) shows an onset in the infrared at *ca.* 1200 nm, a prominent shoulder at *ca.* 500 nm, and a rising absorption edge into the UV, giving the present Ge-NCs their characteristic red color. The gradual onset and increase in the infrared absorption likely results from the appreciable size distribution in the present Ge-NCs as determined from TEM measurements. Photoluminescence (PL) emission was not observed in the present Ge-NCs, as the measured mean diameter is greater than the Bohr exciton radius in bulk Ge and, as such, quantum confinement effects are unappreciable.

The Raman spectrum of free-standing Ge-NCs (Figure 4A) drop-cast from ethanol onto a glass microscope slide shows a single asymmetric peak centered

at  $298.5\text{ cm}^{-1}$  corresponding to the optical phonon (OP) in crystalline Ge. In the bulk crystal, the phonon vibration occurs at a frequency of *ca.*  $302\text{ cm}^{-1}$ , and the shift to lower frequencies in the present sample and the asymmetric broadening are attributed to the phonon confinement effect in the Ge-NCs.<sup>52</sup> The PXRD pattern of the free-standing Ge-NCs drop-cast from ethanol onto a low intensity background Si wafer (Figure 4B) shows intense broad reflections characteristic of diamond structure Ge. Scherrer analysis of the XRD peak broadening provided approximate mean crystal diameters of 14 nm. It should be noted that the absence of the broad feature attributed to amorphous  $\text{SiO}_2$  is consistent with the liberation of the Ge-NCs and etching of the encapsulating matrix. Transmission electron microscopy (TEM) images of Ge-NCs drop-cast onto a holey carbon grid (Figure 4C) show spherical NCs with a measured mean diameter of 17.7 nm ( $n = 448$ ;  $\sigma = 5.5\text{ nm}$ , 31%), in agreement with Scherrer analysis of XRD peak



**Figure 3.** (A) Picture of free-standing, colloiddally stable Ge-NCs in ethanol. (B) Scattering of a red laser from colloiddally stable Ge-NCs in ethanol. (C) Absorption spectrum of Ge-NCs dispersed in ethanol showing an onset at *ca.* 1200 nm, a prominent shoulder at *ca.* 500 nm, and a rising absorption edge into the UV.



**Figure 4.** Characterization of free-standing colloidal stable Ge-NCs. (A) Microscope Raman spectrum of free-standing Ge-NCs drop-cast from ethanol onto a glass microscope slide showing the crystalline Ge optical phonon (OP). (B) Powder X-ray diffraction (PXRD) pattern of Ge-NCs drop-cast onto a low intensity background Si wafer showing reflections characteristic of diamond structure Ge (\* denotes reflections from substrate). (C) Representative transmission electron microscope (TEM) images of Ge-NCs drop-cast from ethanol onto a holey carbon grid. The measured mean diameter was 17.7 nm ( $n = 448$ ;  $\sigma = 5.5$  nm, 31%). (D) High-resolution TEM image showing lattice fringes corresponding to the (111) crystal planes of diamond structure Ge.

broadening. As previously mentioned, the substantial size distribution in the present system is likely the result of compositional inhomogeneities in the sol–gel precursor arising from kinetic differences in TEOS and TEOG hydrolysis and condensation. High-resolution TEM (HRTEM) (Figure 4D) of a single isolated Ge-NC clearly shows crystalline lattice fringes that extend throughout the entire structure and an amorphous surface layer that likely arises from oxide, hydroxide, and alkoxide species. The measured lattice spacing was 0.32 nm corresponding to the (111) crystal plane interlayer spacing in diamond structure Ge.<sup>48</sup> Finally, the composition of the Ge-NCs was verified by energy-dispersive X-ray spectroscopy (EDX) (Supporting Information, S11), which confirms that the NCs are composed predominantly of Ge, with trace O arising from the aforementioned surface species.

The applicability of the present colloidal Ge-NCs as a solution-processable precursor for bottom-up fabrication was demonstrated by the formation of thin films by spin-coating. In order to prepare thin films, a 0.5 wt % solution of Ge-NCs in methanol was spun-cast onto Si

wafers, and the film was characterized by cross-sectional scanning electron microscopy (SEM) and spectroscopic ellipsometry. Methanol was used as the solvent as opposed to ethanol, as the greater volatility produced thicker, higher quality films. In this manner, high quality films of 150 nm thickness were obtained. From the cross-sectional SEM imaging (Figure 5A), it is clear that the film is of even thickness with a uniform surface. The slight texturing of the surface and noticeable porosity arise from the interparticle void spaces, a well-known phenomenon in nanoparticle-based thin films.<sup>42</sup>

In order to determine the thickness as well as the energy dispersion of the real and imaginary parts of the refractive index of the Ge-NC thin films, spectroscopic ellipsometry measurements were performed at an angle of 75° over a wavelength range of 1.27–4.0 eV. A Tauc–Lorentz model, which is based on the Tauc joint density of states and the Lorentz model for the dielectric response for a collection of single atoms, was used for the parametrization of the dielectric function of the Ge-NC thin films.<sup>53</sup> According to the model, if only a single transition is considered, then the imaginary part

of the dielectric function is given by

$$\varepsilon_2(E) \begin{cases} = \frac{AE_0C(E - E_g)^2}{(E^2 - E_0^2)^2 + C^2E^2E} \cdot \frac{1}{E} & \text{when } E > E_g \\ = 0 & \text{when } E < E_g \end{cases} \quad (1)$$

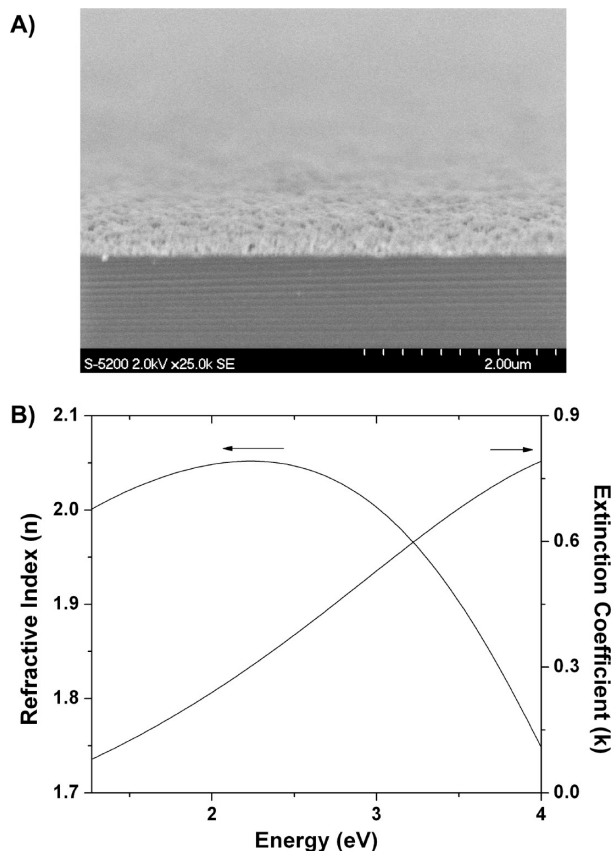
where  $A$  is the amplitude,  $C$  the broadening, and  $E_0$  the central position of the transition.  $E_g$  is the energy gap, and  $\varepsilon_1(\infty)$  is a constant that corresponds to the contribution of transitions outside the measured spectral range. The extinction coefficient  $k$  is readily obtained from  $\varepsilon_2$ , while the real part of the dielectric constant is obtained by Kramers–Kronig integration:

$$\varepsilon_1(E) = \varepsilon_1(\infty) + \frac{2P}{\pi} \int_{E_g}^{\infty} \frac{\xi \varepsilon_2(\xi)}{\xi^2 - E^2} d\xi \quad (2)$$

In this case,  $P$  denotes the Cauchy principal value and  $\xi$  is a function related to the complex angular frequency. The fitting was performed using Levenberg–Marquardt logarithm where six parameters were fitted: the thickness and the four TL parameters. The  $R^2$  value of the regression analysis for the multilayer structure was  $>0.98$ , and the resulting energy dispersion is shown in Figure 5B. It should be mentioned that no Bruggemann effective medium approximation was necessary (typically employed to account for roughened interfaces) in order to improve the statistical measure of the fitting, attesting to the high quality and smoothness of the present films. The most noteworthy features of this energy dispersion are the large  $n$  at infrared wavelengths and the appreciable absorption,  $k$ , throughout the visible as well as UV wavelength ranges. The former is encouraging for the fabrication of bottom-up photonic crystals operating at infrared wavelengths and the latter for the preparation of solution-processable electrical and optoelectronic devices, both ongoing projects in our laboratory.

## CONCLUSION

We have developed a straightforward synthesis for colloidally stable Ge-NCs for use as a solution-processable precursor for the bottom-up fabrication of functional thin films. For the first time, SiO<sub>2</sub>-embedded Ge-NCs are produced by the reductive thermal process-



**Figure 5.** Ge-NC thin film. (A) Representative cross-sectional SEM image of a spun-cast Ge-NC thin film showing a uniform layer thickness and slightly textured surface with noticeable porosity arising from the interparticle void spaces. (B) Refractive index ( $n$ ) and extinction coefficient ( $k$ ) obtained from a Tauc–Lorentz model of the spectroscopic ellipsometric measurements of a spun-cast Ge-NC thin film. The Tauc–Lorentz parameters obtained include the film thickness = 151 nm,  $A = 16.02$ ,  $\varepsilon_1(\infty) = 1.562$  eV,  $E_0 = 4.387$  eV,  $C = 4.439$  eV, and  $E_g = 0.63$  eV.

ing of sol–gel glasses derived from mixtures of tetraethoxyorthogermanate (TEOG) and tetraethoxyorthosilicate (TEOS). A two-step chemical etching protocol was also developed in order to liberate free-standing Ge-NCs from the encapsulating oxide, which demonstrated excellent colloidal stability in alcohol solvents. The applicability of these Ge-NCs as a solution-processable thin film precursor is demonstrated by the fabrication of high refractive index thin films.

## EXPERIMENTAL METHOD

**Reagents and Materials.** Tetraethoxyorthogermanate (TEOG, 99.95%) and tetraethoxyorthosilicate (TEOS, 98%) were purchased from Aldrich and used as received. Anhydrous ethanol was purchased from Brampton and used as received. Hydrochloric acid (HCl<sub>(aq)</sub>, 37%) was obtained from Riedel-de Haën. Hydrogen peroxide (H<sub>2</sub>O<sub>2(aq)</sub>, 35%) and hydrofluoric acid (HF<sub>(aq)</sub>, 48%) were purchased from Caledon and used as received.

**Synthesis of [(GeO<sub>2</sub>)<sub>0.125</sub>(SiO<sub>2</sub>)<sub>0.875</sub>]<sub>n</sub> Sol–Gel Copolymer.** TEOG (3.64 g, 14.4 mmol), TEOS (21.0 g, 100.8 mmol) (1:7 ratio), and anhydrous ethanol (40 mL) were added to a round-bottom flask equipped with a magnetic stir bar, and the solution was gently stirred in air for 30 min to ensure a high degree of mixing. After

this time, aqueous HCl (0.01 M, 20 mL) was added to the solution to catalyze hydrolysis and condensation reactions. The clear and colorless solution turned cloudy white after addition of the HCl solution, and generated a white gel after 48 h. The gel was heated in air at 100 °C in a conventional oven for 48 h and subsequently heated at 600 °C in air for 3 h to complete condensation and dry the solid copolymer. The resulting solid [(GeO<sub>2</sub>)<sub>0.125</sub>(SiO<sub>2</sub>)<sub>0.875</sub>]<sub>n</sub> sol–gel copolymer (7.56 g) was mechanically ground in a mortar and pestle to give a fine white powder.

**Ge-NC/SiO<sub>2</sub> Composite Preparation.** Solid [(GeO<sub>2</sub>)<sub>0.125</sub>(SiO<sub>2</sub>)<sub>0.875</sub>]<sub>n</sub> sol–gel copolymer (2.0 g) was placed in a quartz reaction boat and transferred to a high-temperature tube furnace. The copolymer was heated from 25 to 700 °C at 17 °C/min in a slightly re-

ducing atmosphere (5% H<sub>2</sub>/95% Ar) at which point the temperature was held for 3 h. After cooling to room temperature, the dark red/black powder (1.80 g) was stirred vigorously in a mixture of water (60 mL) and hydrogen peroxide (120 mL) for 30 min to etch bulk unencapsulated Ge. The resulting deep red powder was isolated by centrifugation and washed twice each with water and ethanol and finally dried under flowing N<sub>2</sub> to give bulk Ge-NC/SiO<sub>2</sub> composite (1.53 g).

**Liberation of Ge-NCs.** Free-standing Ge-NCs were liberated from the encapsulating matrix by etching the SiO<sub>2</sub> in a mixture of ethanol and aqueous HF. In a typical experiment, Ge-NC/SiO<sub>2</sub> composite (1.0 g) was stirred in a mixture of water (10 mL), ethanol (10 mL), and 48% HF<sub>(aq)</sub> (10 mL) for 15 min. As the reaction proceeded, the formation of SiF<sub>4(g)</sub> from the etching of SiO<sub>2</sub> by HF was evident. A dark red solid was isolated by centrifugation and washed twice each with water and ethanol to give free-standing Ge-NCs (3 mg), which formed stable deep red colloidal suspensions in ethanol. The final solvent can easily be changed during the last washing steps (e.g., substitute ethanol for methanol).

**Preparation of Ge-NC Films.** In order to prepare thin films, a 0.5 wt % solution of Ge-NCs in methanol was first sonicated for several hours. At the dispensing stage in the spin-coating process, the Ge-NC dispersion was filtered through a 0.7 μm pore Titan 2 GL Microfiber syringe filter to remove any aggregated material. Dispersions were spin-coated at a speed of 1000 rpm for 120 s.

**Characterization.** FTIR spectroscopy was performed on a Perkin-Elmer Spectrum One FTIR spectrometer. Solid [(GeO<sub>2</sub>)<sub>0.125</sub>(SiO<sub>2</sub>)<sub>0.875</sub>]<sub>n</sub> sol-gel copolymer was mixed with KBr, ball milled into a fine powder, and pressed into a dense pellet for analysis. Raman spectroscopy was performed using a 532 nm diode laser and calibrated using a crystalline silicon wafer. X-ray diffraction patterns of all samples were obtained on low intensity background substrates and acquired using a Siemens D5000. Low-resolution and HRTEM imaging and EDX spectroscopy were performed at the Canadian Centre for Electron Microscopy at McMaster University using a FEI Titan 80–300 keV electron microscope. TEM samples of Ge-NCs were drop-cast from an ethanol suspension onto a holey carbon coated copper grid. Absorption spectroscopy of ethanol suspensions of Ge-NCs was performed on a Perkin-Elmer UV/vis/NIR spectrometer Lambda 900. The spin-coater used to deposit films of Ge-NCs was a Laurell WS-400A-6NPP/LITE. Spectroscopic ellipsometry analyses were performed on a Sopra GES-5E ellipsometric porosimeter at a fixed incidence angle of 75° in the range of 1.27–4.0 eV. The modeling and regression of the ellipsometric spectra were performed using the software Winelli II provided by the ellipsometer manufacturer.

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**Supporting Information Available:** Composition of free-standing Ge-NCs. This material is available free of charge via the Internet at <http://pubs.acs.org>.

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